

# Particle in a box (infinite well)

Note

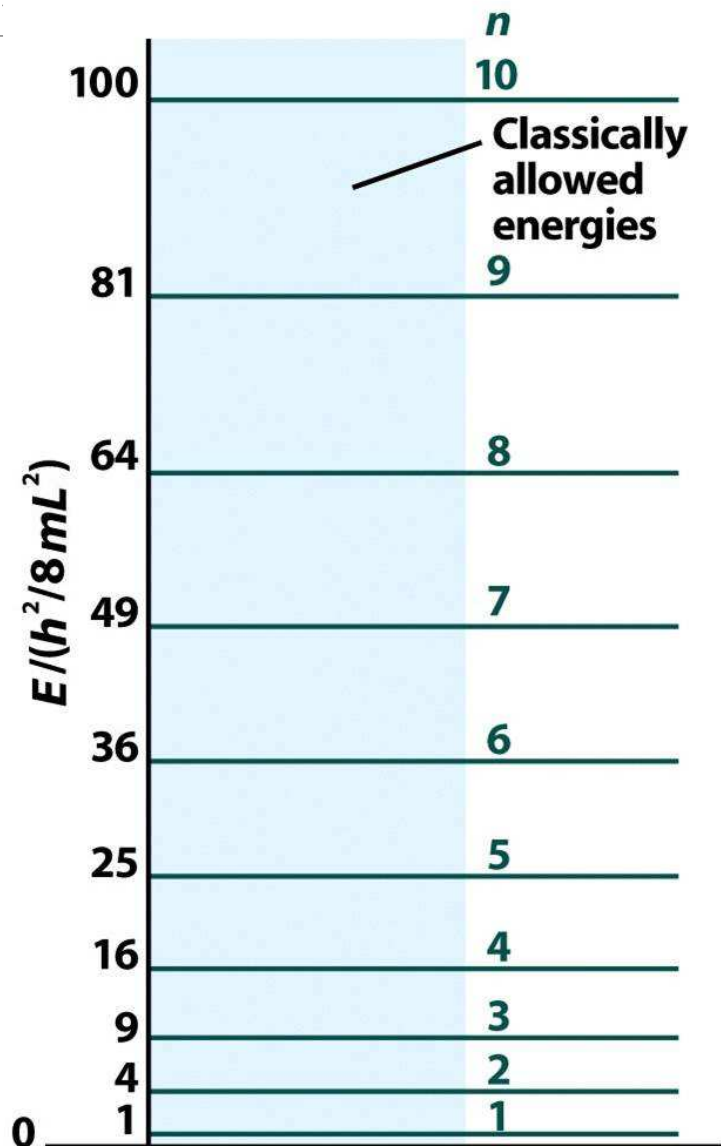
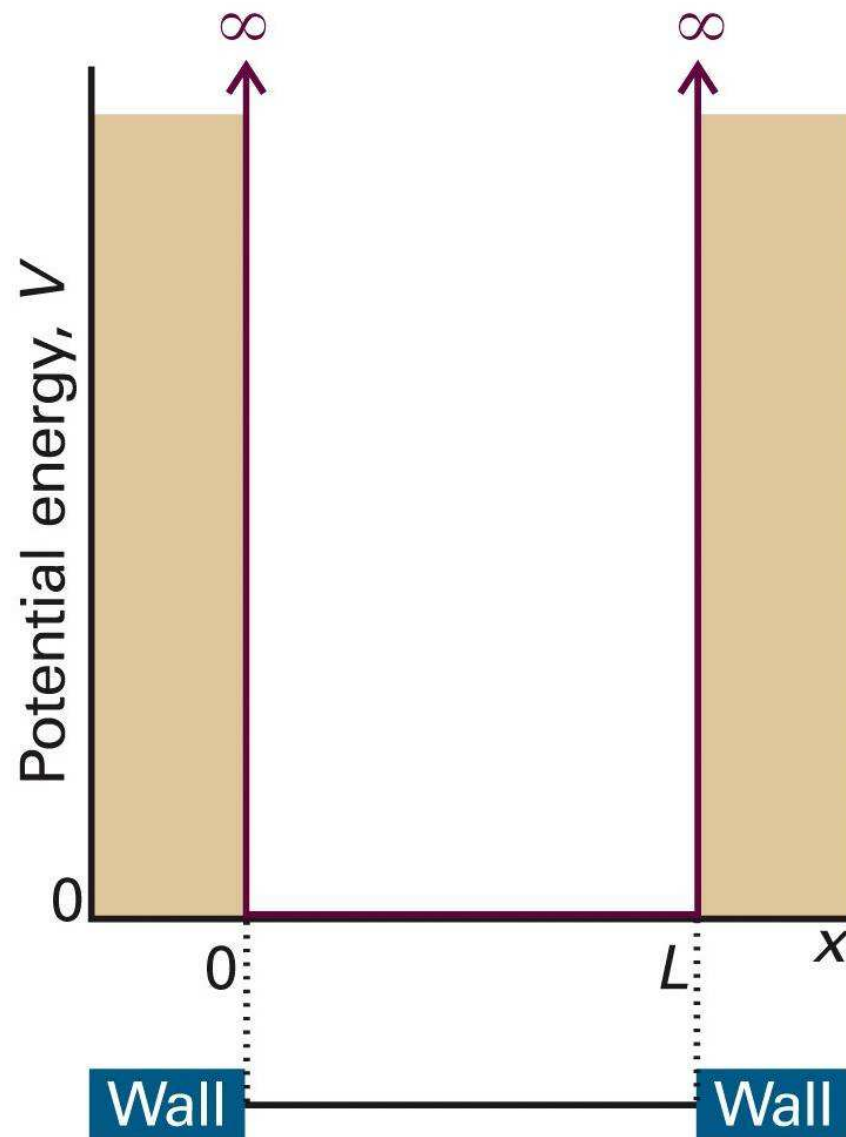


Figure 9-2  
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Figure 9-1  
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Given  $u_n(x) = A \sin(kx) + B \cos(kx)$ ,  
the boundary condition,  $u(0) = 0$ ,  
implies what?

A)  $A = 0$

B)  $B = 0$

C)  $k = 0$

D)  $k = n\pi$ ,  $n = 1, 2, 3 \dots$

E) None of these

Given  $u_n(x) = A \sin(kx)$   
the boundary condition,  $u(a) = 0$ ,  
implies what?

- A)  $A = 0$
- B)  $B = 0$
- C)  $k = 0$
- D)  $k = n\pi$ ,  $n = 1, 2, 3 \dots$
- E) None of these

$$\int f^* \hat{O}_p g dz = \int \underline{(\hat{O}_p f)^*} g dz$$

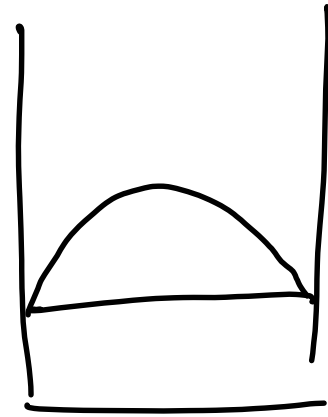
$$\int \psi^* \hat{O}_p \psi dz$$

$$\int f^* g dz = 0$$

$$\psi_n = \sqrt{\frac{2}{L}} \sin\left(\frac{n\pi x}{L}\right) \quad n = 1, 2, 3, \dots$$

$$\langle x \rangle = \int_0^L \psi_1^* x \psi_1 dx = a/2$$

$$\text{Prob} = |\psi|^2 = \psi^2$$



$$\Delta x \Delta p_x \geq \hbar/2$$

$$\Delta x = \sqrt{\langle x^2 \rangle - \langle x \rangle^2}$$

$$\langle x \rangle = \frac{a}{2}$$

$$\Delta p_x = \sqrt{\langle p_x^2 \rangle - \langle p_x \rangle^2}$$

$$\langle p_x \rangle =$$

$$\int \psi_1^* \left( -i\hbar \frac{\partial}{\partial x} \right) \psi_1 dx$$

$$\langle x^2 \rangle = ?$$

$$= 0$$

$$\begin{aligned} \langle p_x^2 \rangle &= \langle 2mE \rangle \\ &= 2m \langle E \rangle \end{aligned}$$

$n$  large

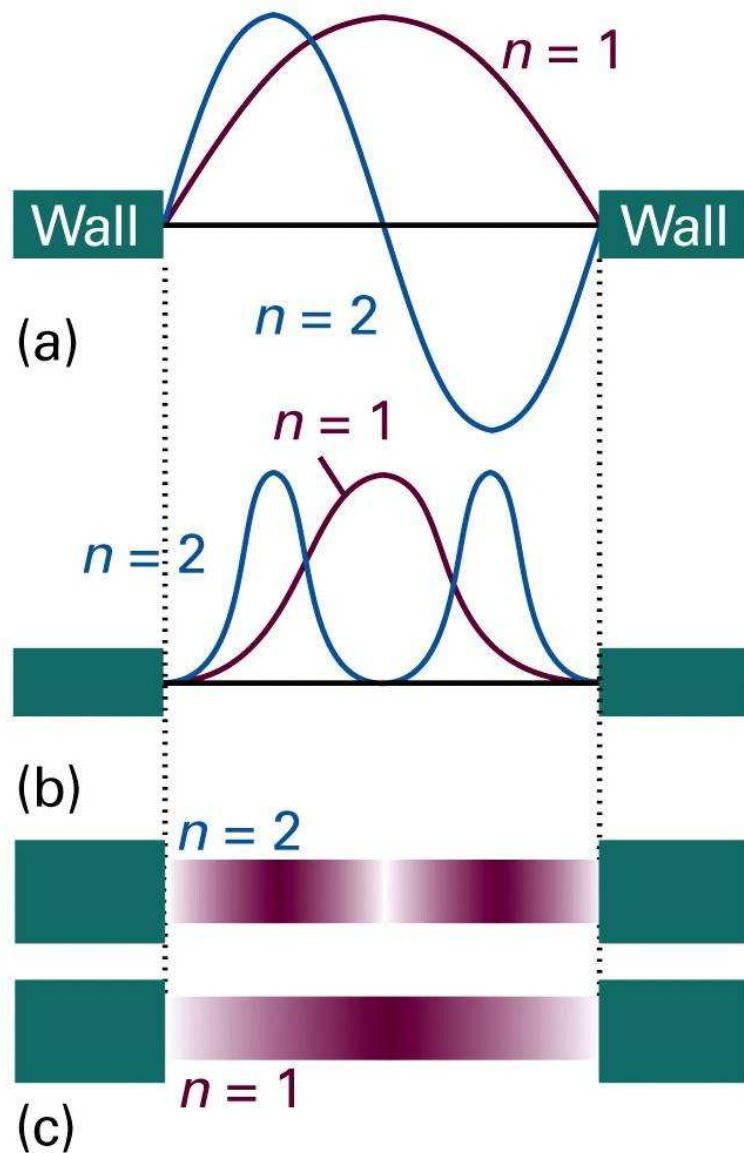
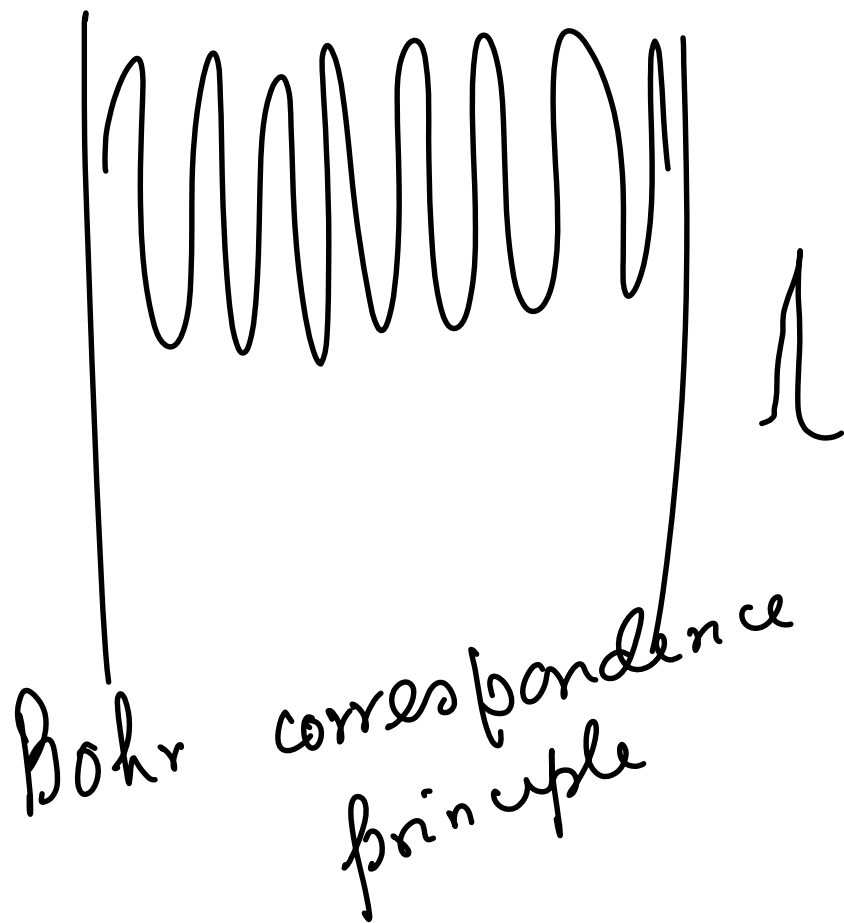
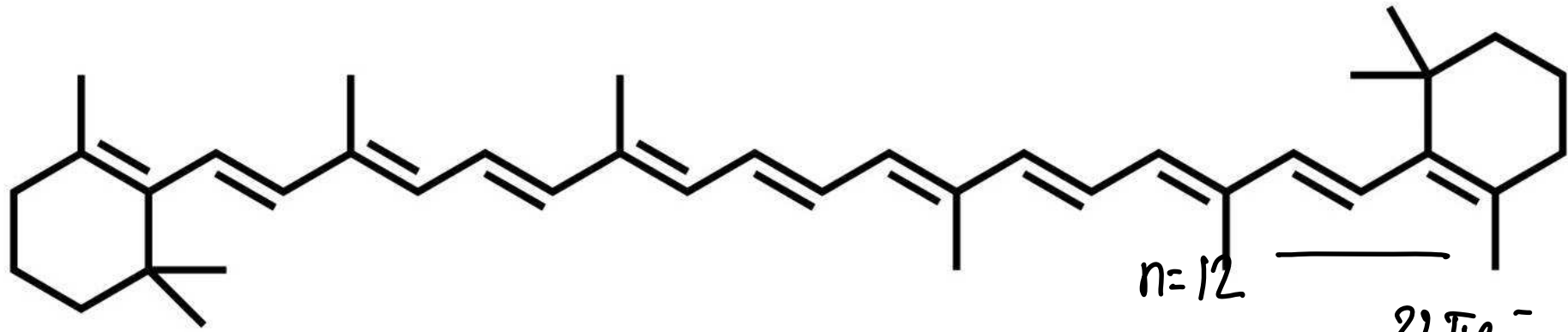


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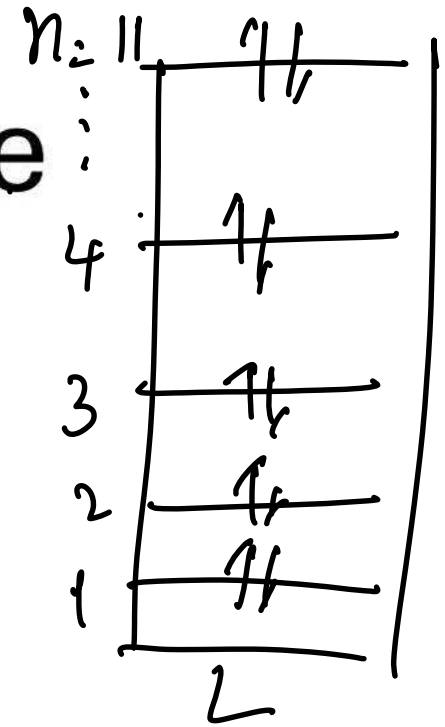
# Optical behavior of carotene



$n=12$

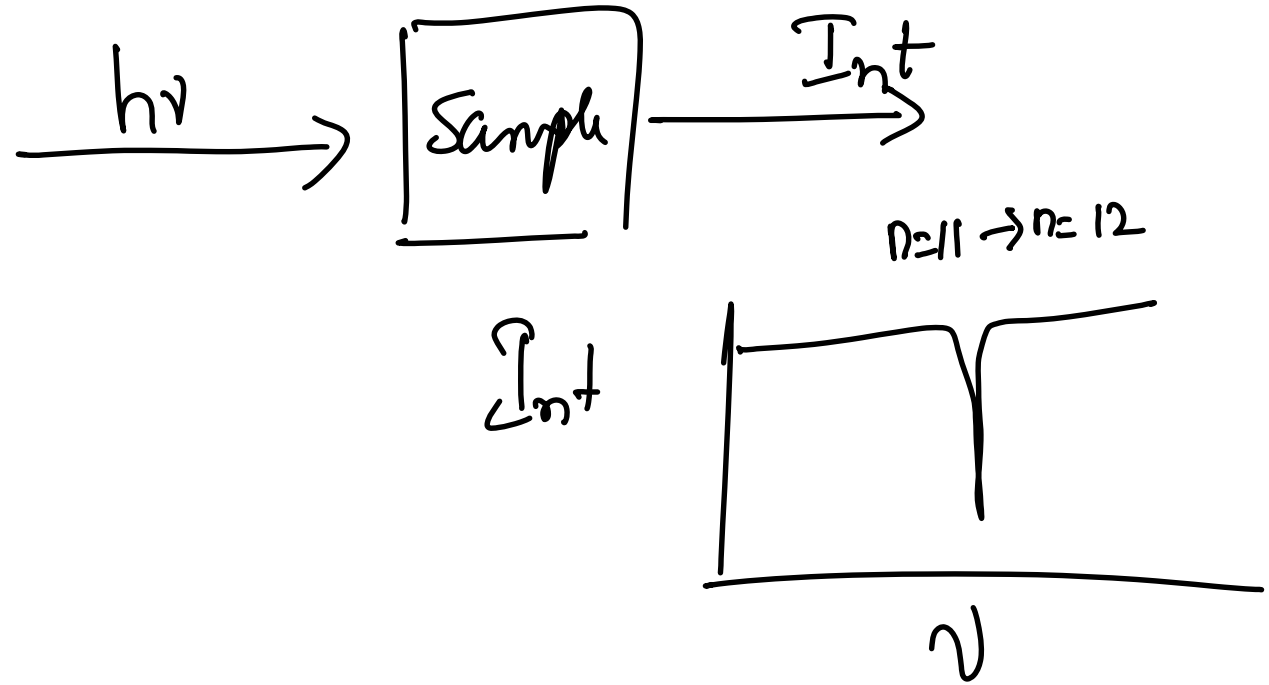
$22\pi e^-$

## 1 $\beta$ -carotene



Marginal 9-1  
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$$-\frac{\hbar^2}{2m_e} \frac{d^2 \psi}{dx^2} = E \psi$$





"  
Porphyrins"  
"

Hemoglobin

$$-\frac{\hbar^2}{2m} \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) \psi(x, y) = E \psi(x, y)$$

$$\boxed{\psi(x, y) = f(x)g(y)}$$

One differential equation  
in  $x$ , & another  
in  $y$

Potential  
energy

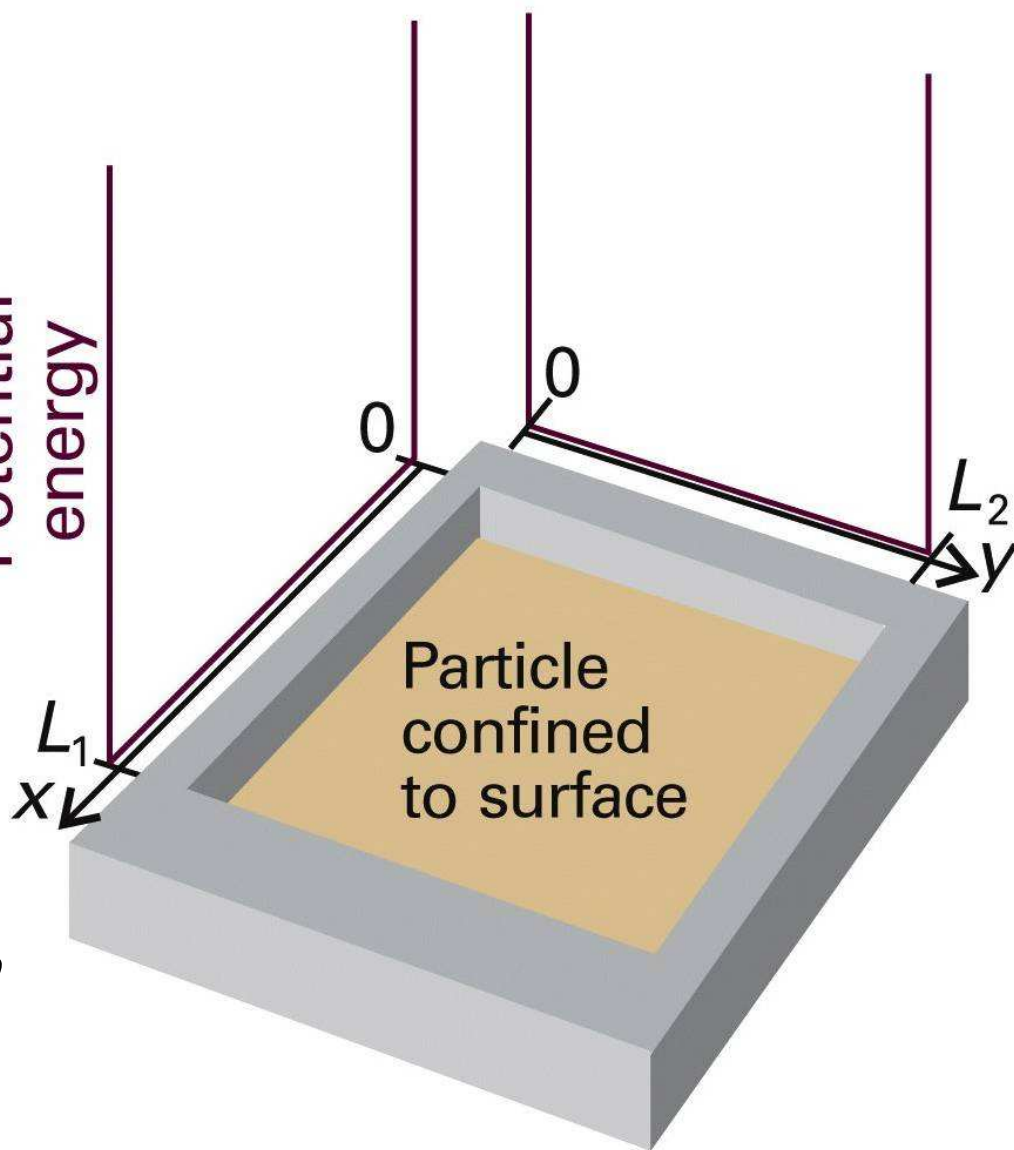


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$$-\frac{\hbar^2}{2m} \left( \frac{d^2}{dx^2} + \frac{d^2}{dy^2} \right) \underbrace{f(x)}_{\phi} \underbrace{g(y)}_{\phi} = E \underbrace{f(x)g(y)}_{\phi}$$

$$\underbrace{\int_x}_{g(y)f(x)} \left( -\frac{\hbar^2}{2m} g(y) \frac{d^2 f}{dx^2} - \frac{\hbar^2}{2m} f(x) \frac{d^2 g}{dy^2} \right) = E f(x)g(y)$$

$\hookrightarrow x$  dependent                       $\hookrightarrow y$ -dependent

$$\hat{H} = \hat{H}_1 + \hat{H}_2 + \hat{H}_3 + \dots$$

$$\hat{H}_1 \psi_1 = E_1 \psi_1$$

$$\hat{H}_2 \psi_2 = E_2 \psi_2$$

o

o

o

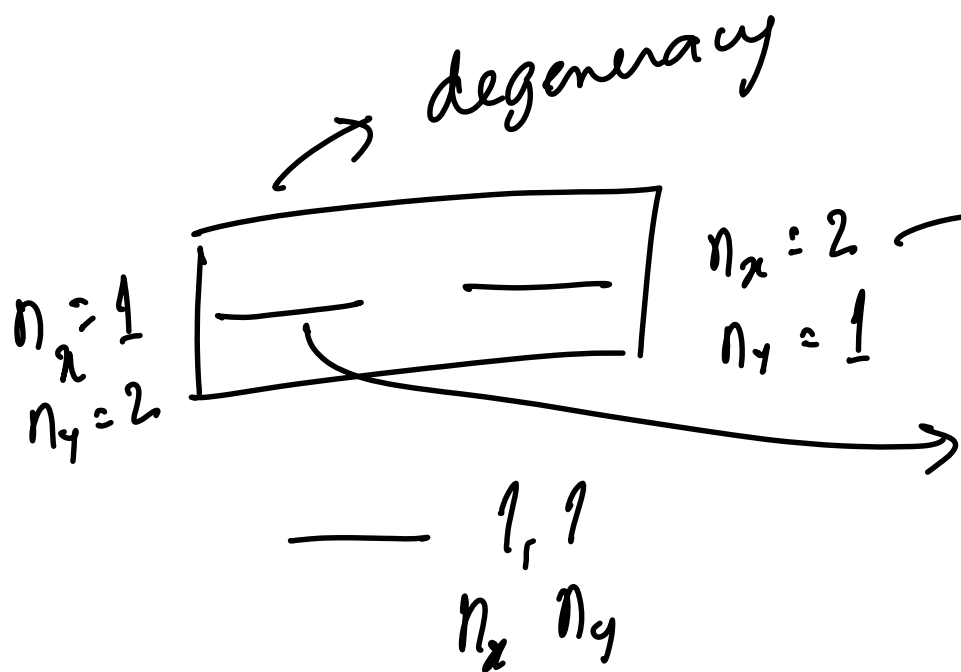
$$\psi = \psi_1 \psi_2 \dots \psi_n$$

$$E = E_1 + E_2 + \dots + E_n$$

$$E = \frac{h^2}{8ma^2} (n_x^2 + n_y^2)$$

$$n_x = 1, 2, 3, \dots$$

$$n_y = 1, 2, 3, \dots$$



$$A \sin\left(\frac{2\pi x}{L}\right) \sin\left(\frac{\pi y}{L}\right)$$

$$A \sin\left(\frac{\pi x}{L}\right) \sin\left(\frac{2\pi y}{L}\right)$$