

$$\begin{aligned}
 c) \quad x(t) &= 2 \sin(25000\pi t) \cos 50\pi t \\
 &= \sin(25050\pi t) \\
 &\quad + \sin(24950\pi t)
 \end{aligned}$$

$$= \sin(2\pi f_1 t) + \sin(2\pi f_2 t)$$

Two sinusoids at $f_1 = \frac{25050}{2} \text{ Hz}$ and
 $f_2 = \frac{24950}{2} \text{ Hz}$.

$$\text{Taking } f_c = \frac{f_1 + f_2}{2} = \frac{25 \text{ kHz}}{2}, \text{ and}$$

$$W = \frac{f_2 - f_1}{2} = 25 \text{ Hz}$$

we have $f_1 = f_c - W$ and $f_2 = f_c + W$

$$\begin{aligned}
 x(t) &= \text{Re} \left(-j e^{j 2\pi (f_c - W)t} \right. \\
 &\quad \left. - j e^{j 2\pi (f_c + W)t} \right)
 \end{aligned}$$

$$\therefore \tilde{x}(t) = -j (e^{j 2\pi f_c t} + e^{-j 2\pi f_c t})$$

$$= -2j \cos 2\pi f_c t$$

$$= -2j \cos 50\pi t$$

One need not always choose f_c to be the midpoint. You can choose f_c to be f_1 or f_2 also, or any other frequency between f_1 and f_2 .