

ELL 788  
Computational Perception & Cognition  
July – November 2015

**Module 4**

Perceiving visual space

# What is space



Space is the theatre where events take place

- Visual space = Visual environment around a person
- Objects: What we act upon
- Environment: Wherein we act / navigate
  - *Described by floor, ceiling, walls, openings (doors / windows), partitions, etc.*

# Perception of space

- Observer-centric
  - *Viewpoint: The space as seen by the observer*
- Two levels of description
  - Structural (geometric)
  - Semantic (what it represents)
    - *e.g. street scene, natural landscape, etc.*
- Perceived in
  - In real 3D world
  - From 2D images

Isovists

# What is an 'Isovist' ?

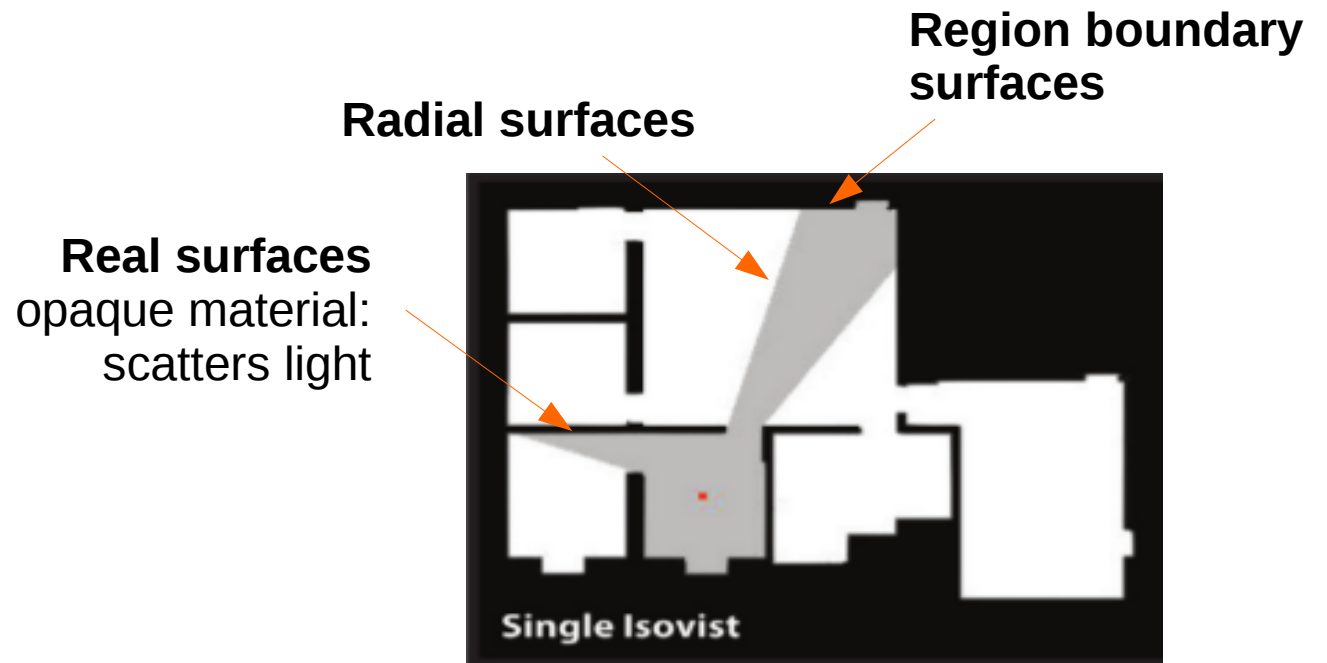
- **View / Viewpoint:** a cone of visible space as seen from an observer's vantage point
  - Orientation
  - Aperture
- **Isovist:** The set of surfaces visible from that location if the observer rotates through 360 degrees



# Isovist: Formal definition

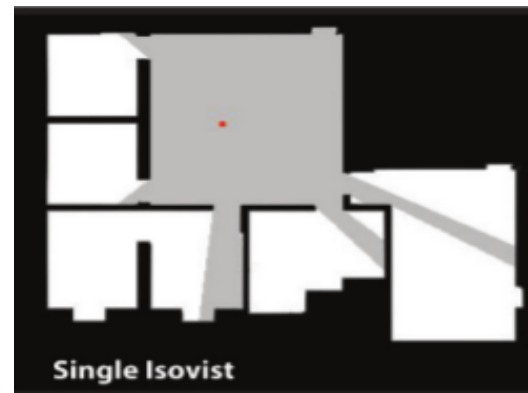
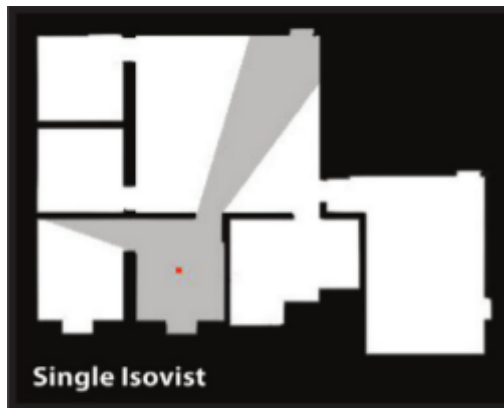
Two alternate definition of isovist:  $V_x$  (x: Vantage point)

- Set of all points in the environment that are visible from x (3D)
- Set of surfaces that are visible from x (2D)



# Isovist map

- A collection (superimposition) of all isovists visible from all possible locations in a space



# Sufficient set and Cardinality number

**How many vantage points are required to see an entire environment E?**

- A finite (usually small) number of vantage points are sufficient
  - The set of isovists is called a **sufficient set**
- The cardinality of smallest sufficient set(s) is called the **cardinality number** for an environment

## Application

- *How many security cameras do you need to cover a retail outlet?*
- *Where do you deploy them ?*



# Minimal path

- Paths connecting vantage points in a sufficient set is called a **sufficient path**
- The sufficient path that is shortest is called a **minimal path**

## Application

*What should be the path taken by a sentry in a museum / residential layout ?*

## Concealment



- Let  $D1$  and  $D2$  be two sub-regions in  $D$ , such that  $D1 \cap D2 = \emptyset$
- Let  $I(D1)$  be the isovist map from  $D1$

- If  $I(D1) \cap D2 = \emptyset$ ,
  - $D2$  is totally invisible (concealed) from  $D1$
- If  $I(D1) \cap D2 \neq \emptyset$ , and  $I(D1) \cap D2 \neq D2$ 
  - $D2$  is partially visible (concealed) from  $D1$
- Assymetrical relation:
  - In general,  $\text{Volume}(I(D1) \cap D2) \neq \text{Volume}(I(D2) \cap D1)$

### Privacy of a space

- *How much you can see without showing your own space*

# Isolation



- Let  $D1$  and  $D2$  be two sub-regions in  $D$ , such that  $D1 \cap D2 = \emptyset$
- Let  $I(D1)$  be the isovist map from  $D1$
- Let  $I(D2)$  be the isovist map from  $D2$

- If  $I(D1) \cap I(D2) = \emptyset$ ,
  - ›  $D1$  and  $D2$  are fully isolated
- If  $I(D1) \cap I(D2) \neq \emptyset$ , and  $I(D1) \cap I(D2) \neq D1 \cup D2$ 
  - ›  $D1$  and  $D2$  are partially isolated

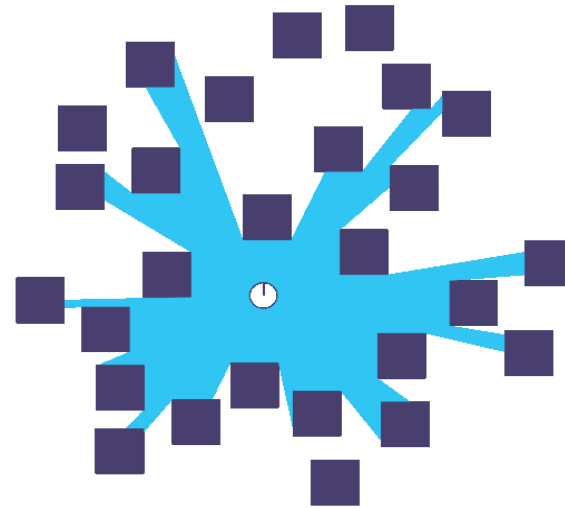
## Architectural design

- *Should the living room be isolated from the kitchen or the bedrooms?*

# Shape of space



Simple isovist



Complex isovist

## Application in architecture

- *The characteristics of an isovist (volume, shape) determines our psychological perception about a closed space*

# Isovist measures

- Consider a planar slice of an isovist
- Consider all radial lines from vantage point ( $x$ ) to the boundary of the environment
  - $l(x, \theta)$  : length of a radial line from  $x$  in direction  $\theta$
- $L_x(\theta)$  is a distribution function of lengths over  $\theta$ 
  - One way to describe an isovist  $V_x$  quantitatively
- Statistical measures  $m(V_x)$  with can be derived
  - Have perceptual significance

- Area (A)
  - How much space can be seen from  $x$
  - From how much space,  $x$  can be seen
- Perimeter (P):
  - How much wall (real surface area) can be seen from  $x$
- Occlusivity (Q):
  - The sum of lengths of the “radial surfaces”
  - Indicator of how much of the environment may be occluded
- Variance and Skewness of  $L_x(\theta)$ :
  - Dispersion and asymmetry of dispersion of the perimeter from the vantage point  $x$
- Circularity (N):
  - Ratio between perimeter-square and  $4\pi$  times area

## How do these measurements relate to human perception and behavior?

- Simple descriptors (area, convexity, perimeter, ...) relates to people's impressions of the spaciousness of hotel lobbies and urban spaces ...
  - *Narrow, cramped, spacious, ample*
- Relates to architectural designs and aesthetics of space
- Guides pedestrian behavior in narrow roads, seating preferences in restaurants ...

[ See Franz, et al. ]

- Isovists do not account for surface properties, such as illumination, color, texture, that are important for perception of space

# Spatial envelop representation



# Describing shape of scenes



- Can we characterize a scene without referring to the individual objects ?
- Can we capture the overall spatial layout and geometry ?

# Spatial envelop representation

- Spatial envelop [architecture]
  - A description of the whole space that provides an “instant impression of the volume of a room or an urban site”
- Spatial envelop representation
  - A formal, computational approach to the capture of the shape of space, as it would be perceived from an observers vantage
  - Can be described by a collection of properties
    - perspective, size, dominant depth, openness, naturalness, ...

# Levels of scene model

- **Subordinate level**

- Scene is treated as a composition of objects, e.g.
- Cars + People + Buildings → City Street,
- Sand + Sea + Sky → Beach

- **Basic level**

- Scenes having similar global visual properties
- e.g., forest, mountain, street

- **Superordinate level**

- Highest level of abstraction, little visual similarity in a class
- e.g., an urban environment, natural landscape



Spatial envelop Representation

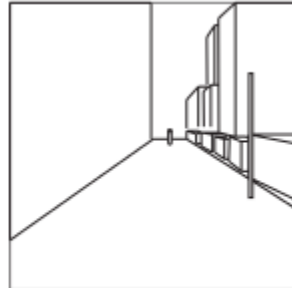
# Properties of scene



Original scene  
"a street"



Suggestive contours  
(Biederman, 1981)



Geometric forms  
(Biederman, 1981)



Blobs in relations  
(Schyns & Oliva, 1994)



Sketch of textures  
(Oliva & Torralba, 2001)

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Boundaries  
(size, shape)

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Contents  
(Texture, color)

# Properties of scene ... more



NATURAL content ← CLOSED spatial layout → URBAN content



NATURAL content ← OPEN spatial layout → URBAN content

*Source: Oliva, et al. 2010*

# Some properties of space

## [Boundaries]

- Openness
  - A horizon line and the lack of visual references
- Expansion (Man-made scene)
  - The convergence of parallel lines gives the perception of the depth gradient of the space.
  - A flat view of a building → low degree of Expansion.
  - A street with long vanishing lines → high degree of Expansion
- Ruggedness (terrain)
  - Deviation of the ground with respect to the horizon
  - Open environments with a flat horizontal ground level vs. mountainous landscapes with a rugged ground
  - Rugged environment produces oblique contours in the picture and hides the horizon line.

# Some properties of space

## [Contents]

- Naturalness
  - Man-made structures: Straight horizontal and vertical lines
  - Natural landscapes: textured zones and undulating contours
- Roughness (for man-made scenes)
  - Size of basic components constituting the scene
  - correlated with the fractal dimension of the scene / its complexity

# 2D image and properties of space

- Spatial envelope properties → visual features of 2D surfaces.
- Thus, the parameters of the spatial envelop can be computed from the statistical distribution of (local) image features
- Spatial envelop is a compressed representation of an image capturing the scene properties



# Computing spatial envelop

## Global and local Texture descriptors

**DFT:**  
**(Global description)**

$$\begin{aligned} I(f_x, f_y) &= \sum_{x,y=0}^{N-1} i(x, y) h(x, y) e^{-j2\pi(f_x x + f_y y)} \\ &= A(f_x, f_y) e^{j\Phi(f_x, f_y)} \end{aligned}$$

**WFT:**  
**(Local Description)**

$$\begin{aligned} I(x, y, f_x, f_y) \\ = \sum_{x',y'=0}^{N-1} i(x', y') h_r(x' - x, y' - y) e^{-j2\pi(f_x x' + f_y y')} \end{aligned}$$

- $H(.,.)$  is a circular Hanning window to take care of the boundary effect
- $\langle A^2, \Phi \rangle$  represents energy spectrum of an image
  - ›  $A^2$  represents energy
  - ›  $\Phi$  represents phase

Use KLT for decomposition and PCA for dimensionality reduction

*Energy Spectrum (global):* 
$$A(f_x, f_y)^2 \simeq \sum_{i=1}^{N_G} v_i \psi_i(f_x, f_y)$$

*Spectrogram (local):* 
$$A(x, y, f_x, f_y)^2 \simeq \sum_{i=1}^{N_L} w_i \Psi_i(x, y, f_x, f_y)$$

$$N_G, N_L < 50$$

$\mathbf{v} = \{v_i\}_{i=1, N_G}$ : Provides a low-resolution global description of an image

$\mathbf{w} = \{w_i\}_{i=1, N_L}$ : Provides a low-resolution description of of an image with spatial arrangement

# Spectral signature

In real-world images, the energy spectra fall in average with a form

$$1 / f^\alpha \quad (\alpha \sim 2)$$

The energy spectrum of different types of images can be approximated by a function

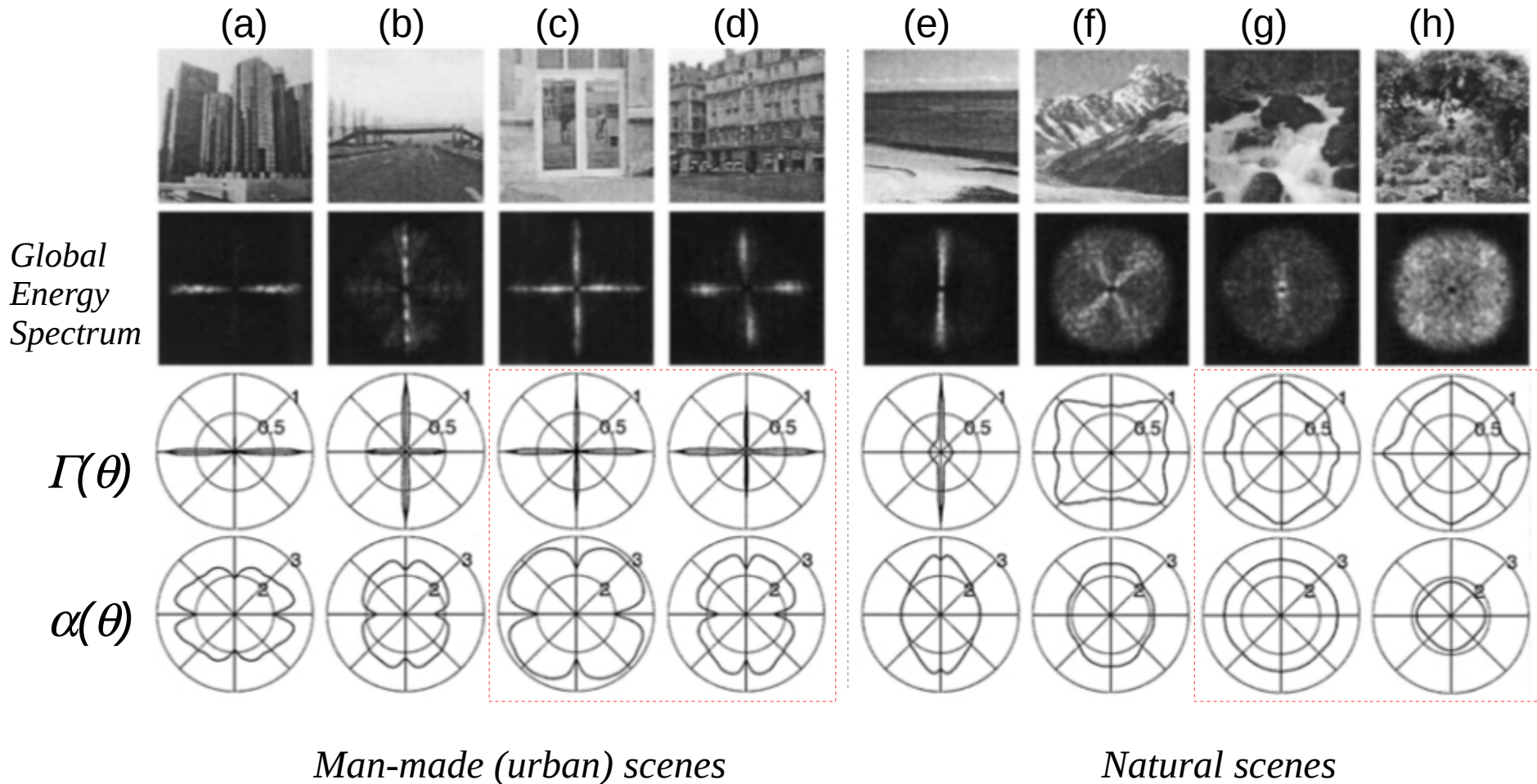
$$E[A(f, \theta)^2 | S] \simeq \Gamma_s(\theta) / f^{-\alpha_s(\theta)}$$

Expected energy spectrum given a category of image  $S$

Parameters estimated through linear regression over a large number of images

- $\Gamma_s(\theta)$ : Dominant orientations of a scene category
- $\alpha_s(\theta)$ : Slope of the decreasing energy spectrum values  
-- related to roughness or complexity of the scene

# Spectral signatures for scene categories



Source: Oliva & Torralba 2001

# Estimation of spatial envelop properties

$\Gamma(\theta)$  and  $\alpha(\theta)$  cannot be easily used to discriminate between properties of scene, e.g. naturalness, openness, etc.

A scene attribute can be expressed as

$$\hat{s} = \mathbf{v}^T \mathbf{d} = \sum^{N_G} v_i d_i$$

The parameters  $d_i$  can be estimated through simple linear regression after arranging many (~500) pictures in order of that attribute

*... And similarly for spectrogram (local descriptors)*

DST: Discriminating Spatial Template (Global)

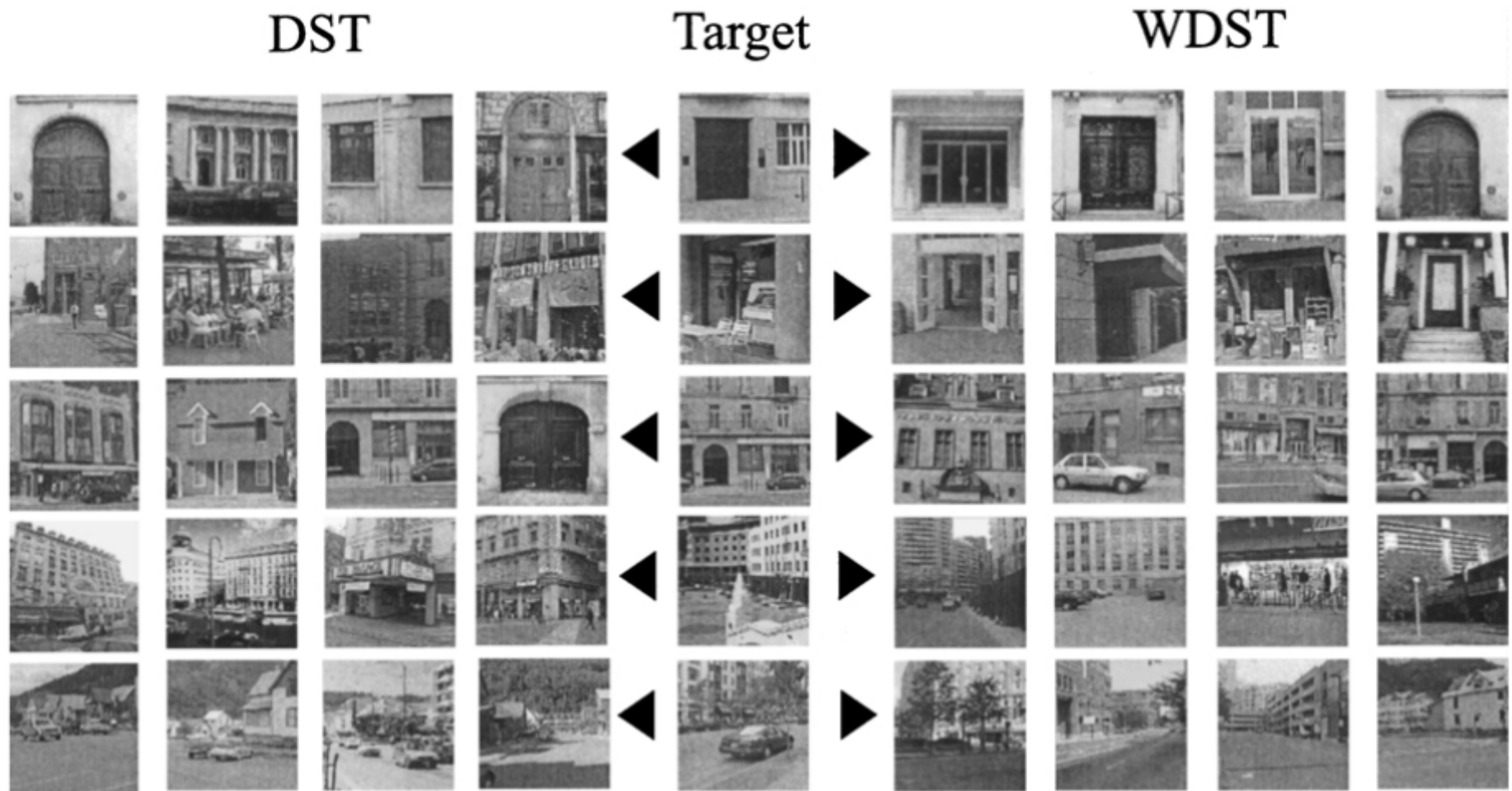
WDST: Windowed Discriminating Spatial Template (Local)

# Example: Openness

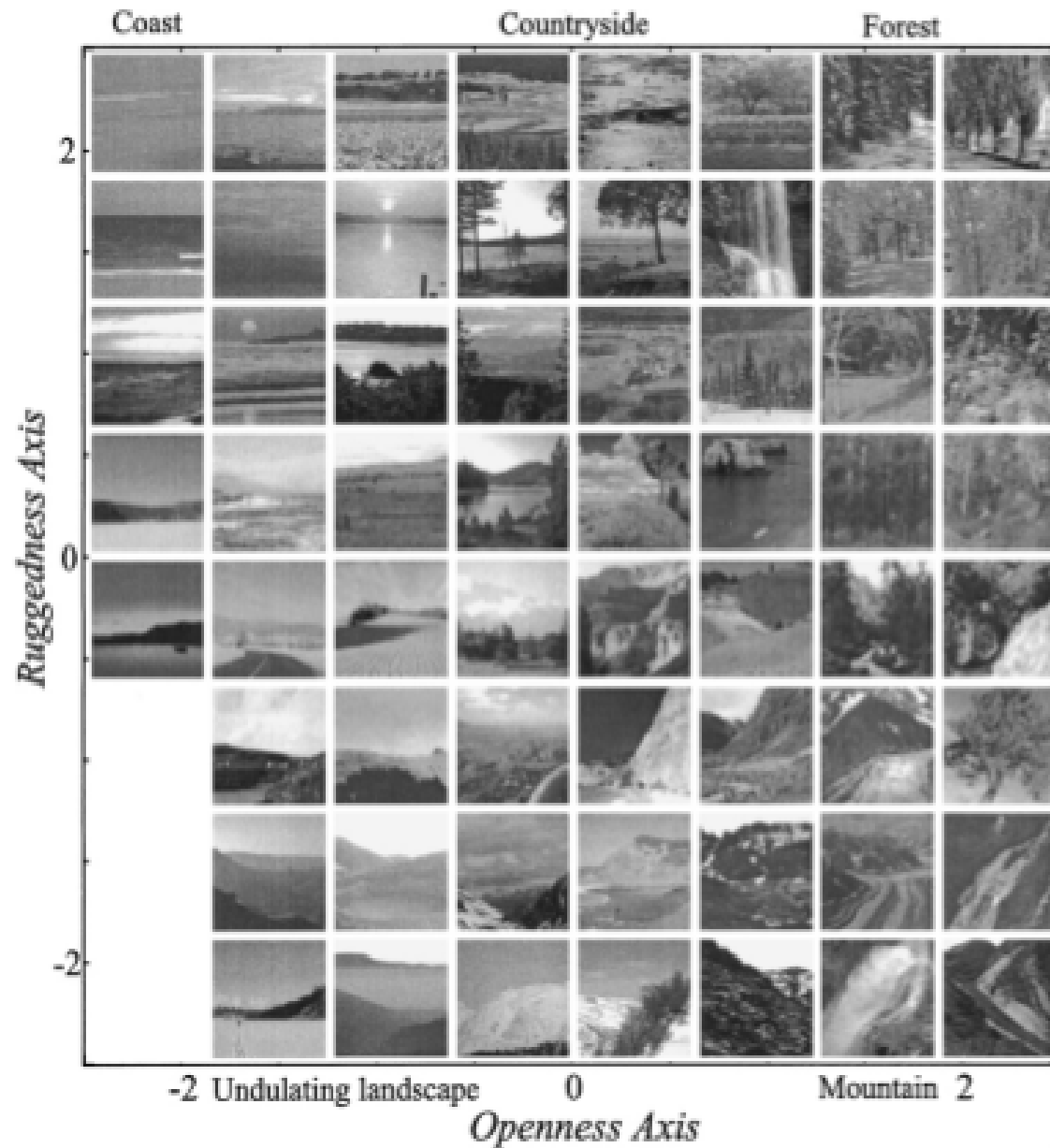


*Source: Oliva, et al. 2010*

# Nearest neighbors (man-made scene) – with DST and WDST



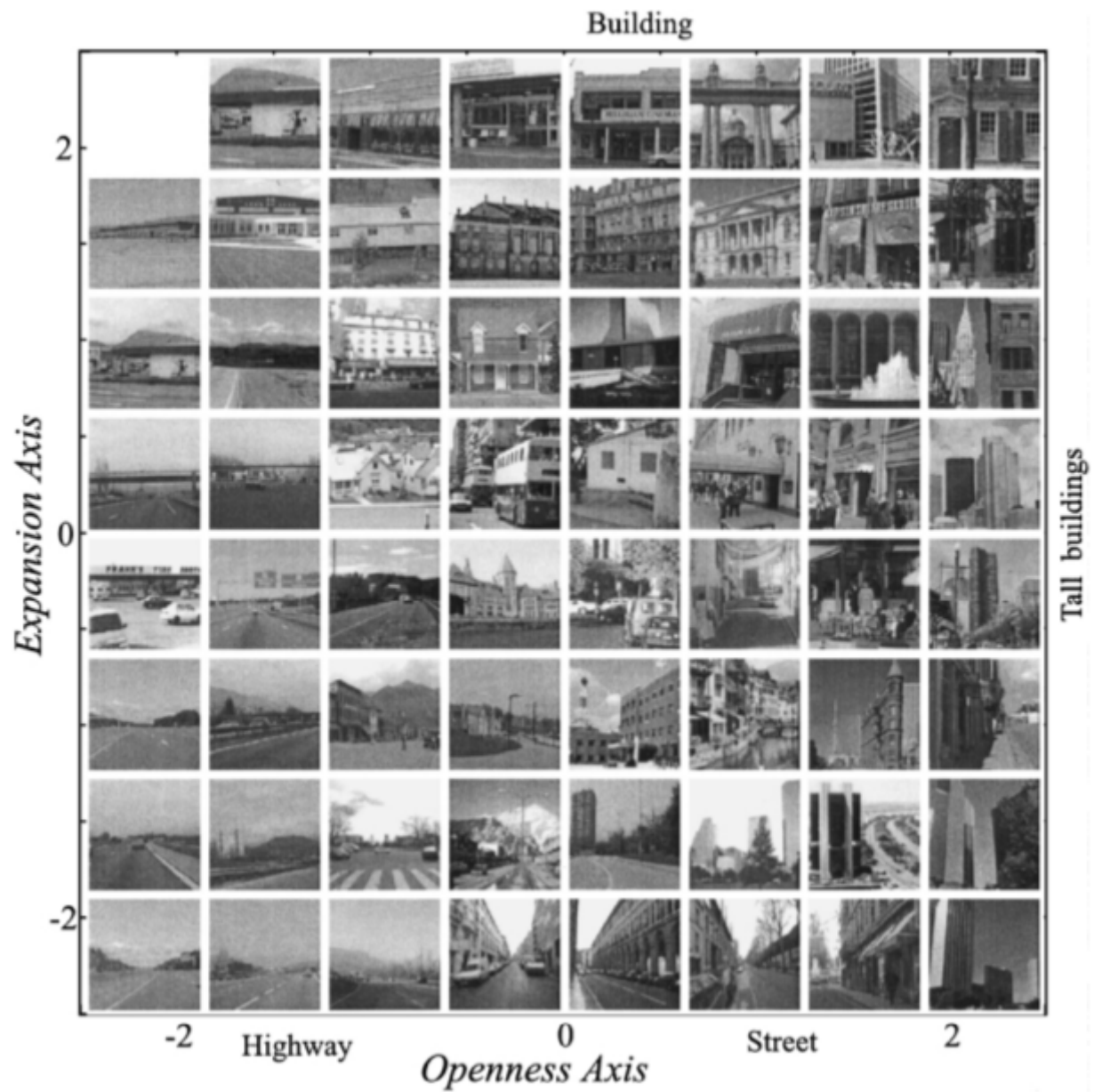
*... WDST generally works better*



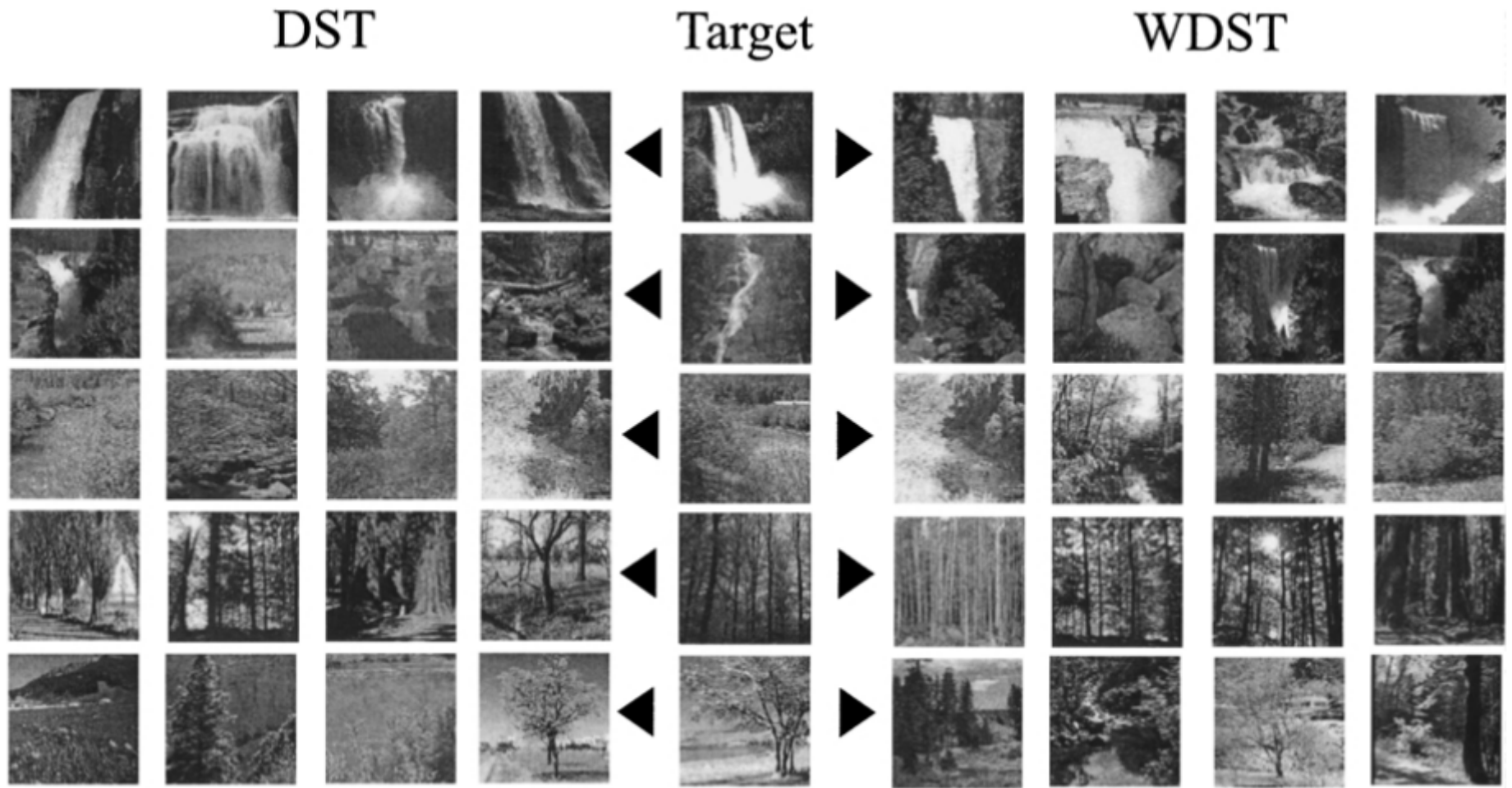
Organization of natural scenes in 2D (using WDST)

Source: Oliva & Torralba 2001



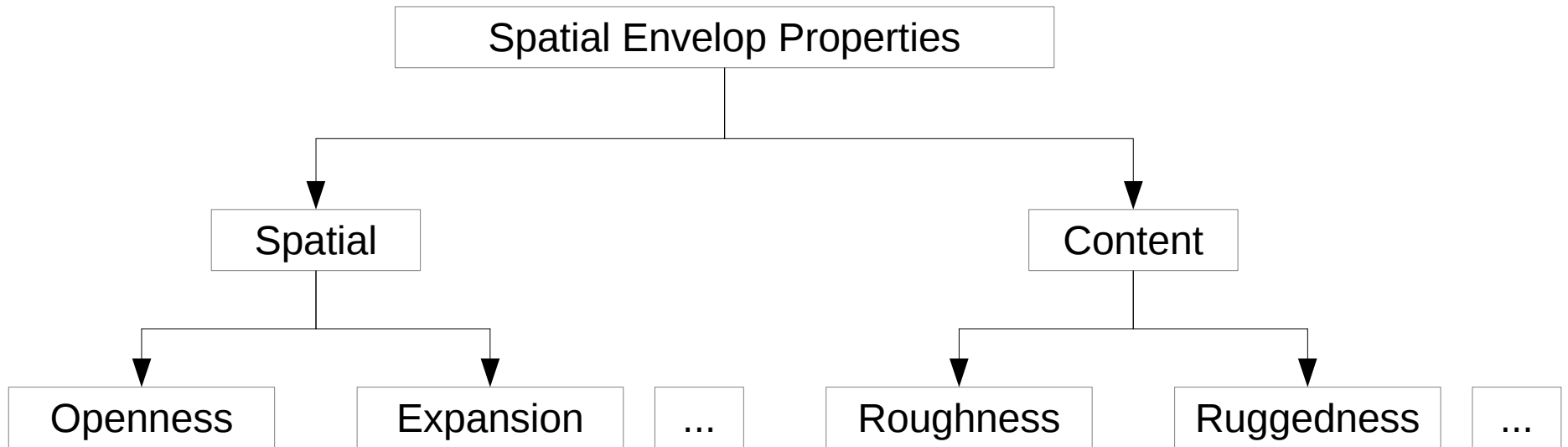


Organization of man-made scenes in 2D (using WDST)



Examples of natural scenes with four neighbors sharing similar spatial envelope, estimated with the DST and the WDST procedures.

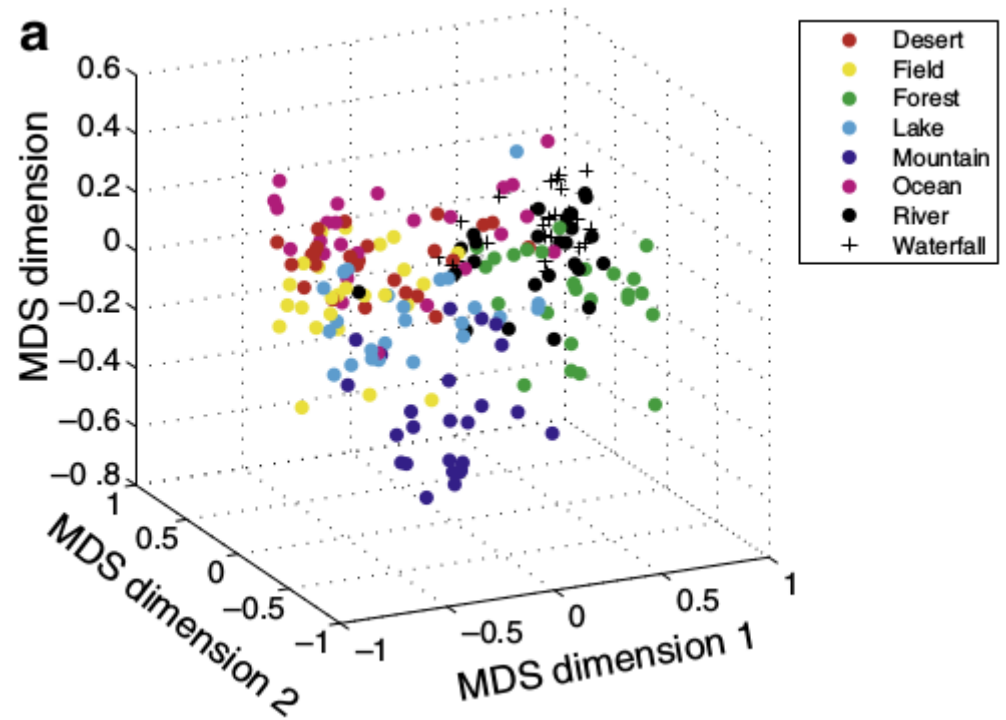
# Summary: Spatial Envelop Representation



## In this framework

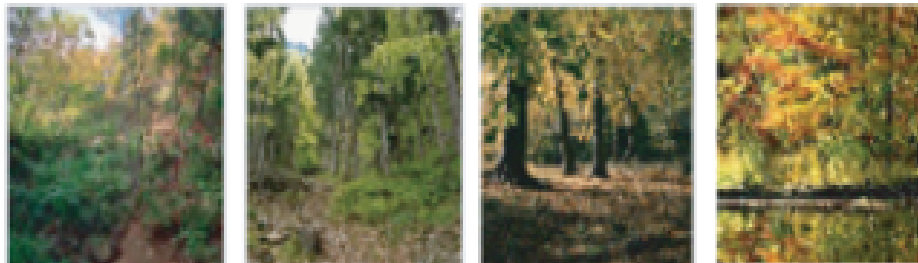
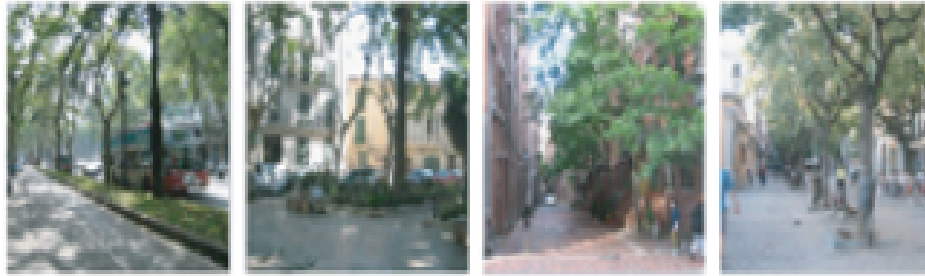
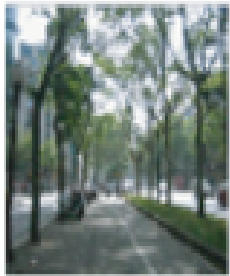
Forest is a natural closed environment with a dense isotropic texture  
**NOT** an environment with trees, bushes and leaves

Semantics of a scene emerges from a multi-dimensional projection on Spatial Envelop axes



Target

Nearest neighbors



Source: Green & Oliva, 2009

Source: Oliva, et al. 2010

- Space centered approach as opposed to object centered approach
  - Space is treated as a material object
- Provides interesting and complementary descriptors for space
  - Quantitative measures relate to perceptual properties
- Isovist
  - describes the visible volumes of a three-dimensional space
- Spatial envelope
  - captures layout and content features from a two-dimensional projected view

# Comparison between Isovist and Spatial Envelope representations

- Space centered approach as opposed to object centered approach
  - Space is treated as a material object
- Provides interesting and complementary descriptors for space
  - Quantitative measures relate to perceptual properties

## **Isovist**

Describes the visible volumes of a three-dimensional space

## **Spatial envelope**

Captures layout and content features from a two-dimensional projected view

# References

- Oliva, Park and Konkale.  
Representing, perceiving, and remembering the shape of visual space  
(Book Chapter), 2010 [overview]
- Benedict. To take hold of space ... 1979 [Isovist]
- Franz, et al.  
Exploring isovist-based correlates of spatial behavior and experience.
- Oliva and Torralba.  
Modeling the Shape of the Scene: ... Spatial Envelope, 2001 [Spatial  
Envelop Representation]