

ELL781: Assignment 3

Submission deadline: **11 November, 23:59**

Maximum Marks: 10

1 Problem statement

This assignment involves implementing the Prim and Kruskal algorithms for finding a Minimum Spanning Tree (MST) of an undirected, weighted graph.

2 Procedure

Here are the steps you should follow for this assignment:

1. *Prim's algorithm*: Start with the Pascal code given in Fig. 7.8 of the *AHU* book. This is essentially what you need to implement, in a programming language of your choice (ideally C/C++/Java). However, one change needs to be made: rather than just taking a cost matrix as input and printing a set of edges as output, you need to take as input and return as output instances of a **GRAPH** data structure. So first of all you need to implement the **GRAPH** Abstract Data Type (ADT) as an actual data structure which allows for weighted, undirected graphs (you are NOT permitted to use existing implementations or libraries). Remember, to fully describe a data structure, you need to specify what your *cells* (atomic data variables) consist of, what the *aggregation mechanism* over those cells is, and what associated operations or *functions* are available to manipulate the data structure. Please structure and document your code so as to show all of these clearly for your data structure corresponding to the **GRAPH** ADT.

Now implement Prim's algorithm using your **GRAPH** data structure. The key point to keep in mind is that your overall implementation needs to be *modular*: a separate **GRAPH** data structure with a defined set of functions/operations, and the main program (for Prim's algorithm) must interact with the data structure only through these functions. **[3]**

2. *Kruskal's algorithm*: Start with the pseudocode given in Fig. 7.10 of *AHU*. As you will notice right away, this is considerably more complicated to implement than Prim's algorithm. In particular, this pseudocode makes use of two new ADTs: **PRIORITYQUEUE** and **MFSET**. So first of all these will need to be implemented. Here is how you should proceed (please follow these steps carefully):

- Implement a **PRIORITYQUEUE** data structure. Please look at Sections 4.10 and 4.11 of *AHU* for details on how this can be done. Your code should be well-commented and it should be easy for anyone reading it to understand how each part works. **[2]**
- Implement an **MFSET** data structure. Look at Section 5.5 of *AHU* to understand what this is and how it can be implemented. There are multiple ways of implementing it, you may pick one as you prefer, but should aim to minimise time complexity. Again, the code should be well-structured and commented for easy readability. **[2]**

- Using both the above data structures, implement Kruskal’s algorithm. Like for Prim’s algorithm, your input and output should be in the form of an instance of your **GRAPH** data structure. [2]
3. Write a top-level program for creating a **GRAPH** instance and running both Prim’s and Kruskal’s algorithms on it, and printing out the respective MSTs returned, along with the total cost and runtime (in milliseconds) for each one. The input to this top-level program should be an $n \times n$ cost matrix for a graph, n being the number of vertices (assume the diagonal elements will always be 0, and elements corresponding to unconnected vertices will be set to -1); this can be read in from a text file. A sample input file is provided at http://web.iitd.ac.in/~sumeet/input_graph.txt, which corresponds to the graph depicted in Fig. 7.4 of *AHU*. [1]

2.1 Output format

Your top-level program should print out the MSTs from the Prim and Kruskal algorithms, in the form of a sequence of $n - 1$ edges (vertex pairs), where n is the number of vertices in the input graph. Each MST should be preceded by a line which gives the name of the algorithm that generated it, the total cost of the MST, and the runtime it took your code to generate the given MST. For the sample input file linked to above, the output might look as follows:

```
Prim’s algorithm MST (total cost: 15; runtime: 17ms)
(1,3)
(2,3)
(2,5)
(3,6)
(4,6)
Kruskal’s algorithm MST (total cost: 15; runtime: 41ms)
(1,3)
(2,3)
(2,5)
(3,6)
(4,6)
```

3 What to submit

You need to submit all your code, properly commented and documented for easy readability as described. Logically, your code should consist of the following 6 components/modules (it is desirable to have each component in a separate file):

- An implementation of a data structure which implements the **GRAPH** ADT.
- An implementation of Prim’s algorithm, as a function which takes a **GRAPH** instance as input and returns another **GRAPH** instance as output.
- An implementation of a data structure which implements the **PRIORITYQUEUE** ADT.
- An implementation of a data structure which implements the **MFSET** ADT.
- An implementation of Kruskal’s algorithm, as a function which uses the above two data structures, and takes a **GRAPH** instance as input and returns another **GRAPH** instance as output.
- A top-level program which is a function that takes as input the cost matrix for a graph in the given format, creates a **GRAPH** instance using it, calls the Prim and Kruskal functions on this instance and gets the **GRAPH** instances returned by each of them (whilst also keeping track of the runtime for each call), and prints out these MSTs in the given format along with the respective total costs and runtimes.

Please package everything into a single zip/tar/rar file. You should also include a README file which explains to the user exactly how they should use your code to generate the MSTs for a given graph.

Submission will be via Moodle; the exact submission procedure will be announced there in due course. The submission deadline for this assignment will be **11 November, 23:59**. Any late submissions will be penalised, and may not be evaluated at all, depending on the extent of delay.

4 Collaboration policy

You are free to discuss any aspect of the assignment with others; however, your code must be entirely written by you, without any copying from anywhere. We will be using plagiarism-detection tools to ensure that this is the case, and any violations will lead to the loss of all marks for the assignment, plus further disciplinary action depending on the severity of the offence.