## Hierarchies in representations Latent structure discovery and Dimensionality reduction



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## Tacit

Knowing
(Thinking fast)
$\rightarrow$

Latent
Relations

## T HVNKING, FAST $\mathrm{T}_{\text {avo }}$ SLOW

D A N I EL
KAHNEMAN

WINNER OF THI NOBEL PRIZE IN ECONOMICS

## Latent Representation



## Manifolds in language

- grounded syntax:

[Nayak and Mukerjee AAAI-12]


## Visuo-Motor expertise

in darkened room, works hard to position arm in a narrow beam of light

Newborns (10-24 days) Small weights tied to wrists

Will resist weights to move the arm they can see

Will let it droop if they can't see it


## Simulation






Robot self-discovery
 discover the world?

## Camera Motion and Shape via Factorization

## Homogeneous Coordinates

- 2-D point ( $x, y$ ) represented as $\left(x_{1}, x_{2}, x_{3}\right)$ in homogeneous system

$$
x=x_{1} / x_{3} \quad y=x_{2} / x_{3}
$$

- $\left(\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}\right)$ same as $\left(\mathrm{kx}_{1}, \mathrm{kx}_{2}, \mathrm{kx}_{3}\right)$ same as $\left(\mathrm{x}_{1} / \mathrm{x}_{3}, \mathrm{x}_{2} / \mathrm{x}_{3}, 1\right)$
- Similarly for 3-D point - $\left(\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}, \mathrm{x}_{4}\right)$


## Camera Models

- Orthographic
- Weak perspective/Scaled orthographic
- Para-perspective
- Perspective
- Affine
- Projective


## Camera Models

- $x=(u, v, 1)^{\top}$ or $\left(x_{1}, x_{2}, x_{3}\right)^{\top}=>$ homogeneous image coordinates
- $X=(x, y, z, 1)^{\top}$ or $\left(X_{1}, X_{2}, X_{3}, X_{4}\right)=>$ homogeneous 3D coordinates

$$
X_{(3 \times 1)}=T_{(3 \times 4)} X_{(4 \times 1)}
$$

$$
\left[\begin{array}{l}
x_{1} \\
x_{2} \\
x_{3}
\end{array}\right]=\left[\begin{array}{llll}
T_{11} & T_{12} & T_{13} & T_{14} \\
T_{21} & T_{22} & T_{23} & T_{24} \\
T_{31} & T_{32} & T_{33} & T_{34}
\end{array}\right]\left[\begin{array}{c}
X_{1} \\
X_{2} \\
X_{3} \\
X_{4}
\end{array}\right]
$$

## Orthographic Camera Model



$$
u=x \quad v=y
$$

## Orthographic Camera Model

$$
\begin{gathered}
\mathbf{T}_{\text {orth }}=\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1
\end{array}\right] \\
{\left[\begin{array}{l}
x_{1} \\
x_{2} \\
x_{3}
\end{array}\right]=\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]\left[\begin{array}{l}
X_{1} \\
X_{2} \\
X_{3} \\
X_{4}
\end{array}\right]}
\end{gathered}
$$

## Perspective Camera Model



## Perspective Camera Model

$$
\begin{gathered}
\mathbf{T}_{p}=\left[\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 / f & 0
\end{array}\right] \\
{\left[\begin{array}{l}
x_{1} \\
x_{2} \\
x_{3}
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 / f & 0
\end{array}\right]\left[\begin{array}{c}
X_{1} \\
X_{2} \\
X_{3} \\
X_{4}
\end{array}\right]}
\end{gathered}
$$

## Weak Perspective or Scaled Orthographic

$$
\begin{aligned}
& \mathbf{T}_{w p}=\left[\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & Z_{\text {ave }} / f
\end{array}\right] \\
& {\left[\begin{array}{c}
x_{1} \\
x_{2} \\
x_{3}
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & Z_{\text {ave }} / f
\end{array}\right]\left[\begin{array}{c}
X_{1} \\
X_{2} \\
X_{3} \\
X_{4}
\end{array}\right] }
\end{aligned}
$$

## Affine Camera Model

$$
\begin{aligned}
\mathbf{T} & =\left[\begin{array}{cccc}
T_{11} & T_{12} & T_{13} & T_{14} \\
T_{21} & T_{22} & T_{23} & T_{24} \\
0 & 0 & 0 & T_{34}
\end{array}\right] \\
{\left[\begin{array}{l}
x_{1} \\
x_{2} \\
x_{3}
\end{array}\right] } & =\left[\begin{array}{cccc}
T_{11} & T_{12} & T_{13} & T_{14} \\
T_{21} & T_{22} & T_{23} & T_{24} \\
0 & 0 & 0 & T_{34}
\end{array}\right]\left[\begin{array}{l}
X_{1} \\
X_{2} \\
X_{3} \\
X_{4}
\end{array}\right]
\end{aligned}
$$

## Projective Camera

$$
\begin{aligned}
& \mathbf{T}=\left[\begin{array}{llll}
T_{11} & T_{12} & T_{13} & T_{14} \\
T_{21} & T_{22} & T_{23} & T_{24} \\
T_{31} & T_{32} & T_{33} & T_{34}
\end{array}\right] \\
& {\left[\begin{array}{l}
x_{1} \\
x_{2} \\
x_{3}
\end{array}\right]=\left[\begin{array}{llll}
T_{11} & T_{12} & T_{13} & T_{14} \\
T_{21} & T_{22} & T_{23} & T_{24} \\
T_{31} & T_{32} & T_{33} & T_{34}
\end{array}\right]\left[\begin{array}{c}
X_{1} \\
X_{2} \\
X_{3} \\
X_{4}
\end{array}\right] }
\end{aligned}
$$

# Structure from Motion by Factorization 

 streams under orthography: a factorization method.
## Factorization Method

- Given: Image stream, where P points have been tracked over F frames
- Image coordinates of $p$-th point in $f$-th frame $=u_{f p}, v_{f p}$
- $\mathbf{W}=2 \mathrm{~F} \times \mathrm{P}$ Measurement Matrix
- Column => observation for point Row => observation for frame

$$
W=\left[\begin{array}{ccc}
u_{11} & \ldots & u_{1 P} \\
\ldots & \ldots & \cdots \\
u_{F 1} & \ldots & u_{F P} \\
V_{11} & \ldots & v_{1 P} \\
\cdots & \ldots & \cdots \\
v_{F 1} & \cdots & V_{F P}
\end{array}\right]
$$

## Factorization Method : Orthography

- $\mathbf{W}=\mathbf{M}_{(2 F \times 3)} \mathbf{S}_{(3 \times P)}+\mathbf{t}_{(2 \times x 1)}[1 \ldots 1]_{(1 \times P)}$ translation vector $\mathbf{t}$ : element $f=$ mean of $\operatorname{row} f$ in $\mathbf{W}$
- registered measurement matrix $\mathrm{W}^{*}$

$$
\mathbf{W}^{*}=\mathbf{W}-\mathbf{t}[1 \ldots 1]=\mathbf{M} \mathbf{S} \quad(\operatorname{rank} 3)
$$

$\mathbf{M}_{(2 F \times 3)}$ : row $f=$ camera horiz/ vert axes in frame $f$ $\mathbf{S}_{(3 \mathrm{xP})}$ : column $p=(\mathrm{x}, \mathrm{y}, \mathrm{z})$ of tracked point $p$

OBJECTIVE : obtain $\mathbf{M}$ and $\mathbf{S}$ from $\mathrm{W}^{*}$ via SVD

## Hotel Stream Data


frame 1

## Hotel Stream Data


frame 50

## Hotel Stream Data


frame 100

## Tracked Features



## Tracking



## Factorizataion Method : Orthography

- Creation of measurement matrix W
- Obtaining registered measurement matrix $\mathbf{W}^{*}$
- Performing SVD to obtain

$$
\mathbf{W}^{*}=\mathbf{U E V}^{\top}=\mathbf{M S}
$$

- $\mathrm{M}=\mathrm{UE}^{0.5} \quad \mathrm{~S}=\mathrm{E}^{0.5} \mathrm{~V}^{\top}$...not unique solution
- MS or $\left(\mathrm{M}_{2} \mathrm{~A}\right)\left(\mathrm{A}^{-1} \mathrm{~S}_{2}\right)$...both are solutions
- Constraints to obtain unique A
- Directions can be aligned to camera directions in first frame


## SVD



## Camera Motion Estimation [M]

camera yaw (degrees)


## Camera Motion Estimation [M]

 camera pitch (degrees)
error < 0.35 degrees

## 3D Shape Estimation [S]



## Multi-body Factorization Method

- Multiple objects in a video sequence moving independently
- Earlier approach => from object frame (as if object stationary and camera moving)
- Common representation required for all objects in multiobject scenario
- Why not look from camera frame!!!
- (Moving camera+static object) equivalent to (static camera +moving object)
- unique for all objects for a frame


## Multi-body Factorization Method

- Points from all objects collectively taken
- Expected Rank <= 4*number of objects
- Shape Interaction Matrix

$$
\mathbf{Q}=\mathbf{V} \mathbf{V}^{\top}
$$

- Q independent of camera orientation, coordinate transformation
- Permuting columns of $V$ does not change values of $Q$ matrix(only row/column number changed in same way as V permutation)
- Only the interaction values of points from same object get non-zero value.
- Block-diagonalization to obtain the points corresponding to same object


## Multi-body Factorization Method



## Aspects of Factorization

- All images treated uniformly
- Alternate approaches are initialization based and may do poorly if improper.
- Convergence guaranteed by numerical approach
- In multi-object factorization, can determine number of objects and point clusters


# Unsupervised Action Learning and Anomaly Detection 

### 3.2. Topic Modelling

- Given: Document and Vocabulary
* Document is histogram over vocabulary
- Goal: Identify topics in a given set of Documents

Idea: Topics are latent variables

Alternate view :

- Clustering in topic space
- Dimensionality reduction


### 3.3. Models in practice

- LSA

Non-parametric clustering into topics using SVD.

- pLSA:

Learns probability distribution over fixed number of topics; Graphical model based approach.

- LDA :

Extension of pLSA with dirichlet prior for topic distribution. Fully generative model.

## 4. Vision to NLP : Notations

| Text Analysis | Video Analysis |
| :--- | :--- |
| Vocabulary of words | Vocabulary of visual words |
| Text documents | Video clips |
| Topics | Actions/Events |

### 5.1. Video Clips

- 45 minute video footage of traffic available
- 25 frames per second
- 4 kinds of anomaly
- Divided into clips of fixed size of say $4-6$ seconds


### 5.2. Visual Words

- Each frame is $288 \times 360$
- Frame is divided into $15 \times 18$ parts, each part containing 400 pixels
- Features
- Optical flow
- Object size
- Background subtraction is performed on each frame to obtain the objects in foreground. Features are computed only for these objects
- Foreground objects consist of vehicles, pedestrians and cyclists


### 5.2. Visual Words (contd..)

- Foreground pixels then divided into "big" and "small" blobs (connected components)
- Optical flow computed on foreground
- Flow vector quantised into 5 values :
- Static
- Dynamic- up, down, left and right
- $15 \times 28 \times 5 \times 2$ different "words" obtained


### 5.3. Foreground Extraction



### 5.4. Optical Flow: Heat Map



## 6. Modelling pLSA

- Training Dataset: no or very less "anomaly"
- Test Dataset: usual + anomalous events

Procedure

- Learn $P(w \mid z)$ and $P(z \mid d)$ from training data
- Keeping $P(w \mid z)$, estimate $P(z \mid d)$ on test data
- Threshold on likelihood estimate of individual test video clips


## 7. Results Demo

- 3 clips
- 3 different types of anomalies


## 8. Results (ROC plot)



## 8. Results (PR curve)



## Motion Planning

## Motion planning

Given start / goal image, map to manifold using local interpolation

Use k-nn connectivity in manifold as "roadmap" for motion planning


## Obstacle modeling by node deletion



If obstacle intersects robot in image space $\rightarrow$ delete corresponding nodes from "visual roadmap"

## Path planning as obstacle moves



## Mobile robots



## Residual error : disk robot



## Robot Motion Planning

Destination

Source

# Path Planning Interface 




Real robots

## SCARA arm



## SCARA arm : degrees of freedom



## Background Subtraction : Robot

 image
foreground (moving part)

learned background

## Background Subtraction : Obstacle



$$
114
$$

## Visual Configuration Space




Application to Graphics

## Head Motion


[M. S. Ramaiah, Ankit Viiay, Geetika Sharma, Amitabha Mukeriee IEEE VR-13]

## Minimal Commitment Language Acquisition

## Previous Work: Unsupervised Semantics

- single word or phrase learning [no grammar]
- Hand-coded propositional (T/F) semantics
- [plunkett etal 92]
- [regier 96] (prepositions)
- [steels 03] [roy/reiter 05] [caza/knott 12]
- Supervised Learning of semantics
- [kate/mooney 06] : set of predicates are known
- [yu/ballard 07] : semantics = scene-region
- Unsupervised Semantic Acquisition :
"right" granularity for concepts; dynamic predicates


## What is a Symbol?

- grounded lexicon:



## Lexicon

- grounded lexicon:

- semantic pole : perceptual patterns (image schemas) $\rightarrow$ probabilistic predicate + arguments


## Grammar

- grounded syntax:



## Minimal Commitment

- minimize prior knowledge in agent:
- preference: minimize description lengths
$\rightarrow$ inventory of machine learning algorithms
- no knowledge of grammar - no POS tags, no syntactic structure
- no knowledge of domain
- bootstrapping stage:
- semantic schemas come first
- language regularities later


## POS categories are discovered

$\left[\begin{array}{c}\text { ball } \\ \text { block } \\ \text { box } \\ \text { circle } \\ \text { square }\end{array}\right]\left[\begin{array}{c}\text { in } \\ \text { inside } \\ \text { into }\end{array}\right]\left[\begin{array}{c}\text { chases } \\ \text { pushes } \\ \text { corners } \\ \text { the }\end{array}\right]\left[\begin{array}{c}\text { big } \\ \text { large } \\ \text { little } \\ \text { the }\end{array}\right]$

## Acquisition Domains

## Previous Work: Unsupervised Semantics

- single word or phrase learning [no grammar]
- Hand-coded propositional (T/F) semantics
- [plunkett etal 92]
- [regier 96] (prepositions)
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- Supervised Learning of semantics
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- Unsupervised Semantic Acquisition :
"right" granularity for concepts; dynamic predicates


## Previous Work: Grammar

- Grammar learning:
- Grammatical categories:
- [redington etal 98] (RNN)
- [wang / mintz 07] (frequent frame)
- Grammar induction : Structure is known
- No semantics:
- [marino etal 07] [solan edelman 05]
- Propositional semantics
- [kwiatkowski zettlemoyer 10] (SVM)
- [kim/moonev 12] (altered visual input)


## Language Acquisition : Domain 1

- Perceptual input

- Discovery Targets:
- semantics: objects, 2-agent actions, relations
- lexicon : nominal, transitive verbs, preposition
- lexical categories: N VT P Adj
- constructions: PP VP S
- sense extension (metaphor) [nayak/mukerjee (AAAI-12)]


## Language Acquisition : Domain 2

- Perceptual input

- Discovery Targets:
- semantics: object categories, motion categories


## Language Acquisition : Domain 2

- object categories

- Discovery Targets:
- semantics: object categories, motion categories
- lexicon : word boundaries, nominals, intransitive verbs
- construction intransitive V/P


## Video Fragment



## Discovering Language

- Perceptual structure discovery:
- Given perceptual space $W$ discover set of structures $\Gamma$ that partition it into patterns relevant to agents goals.
- Elements $\gamma \in \Gamma$ constitute a hierarchy; structures learned earlier are used for more complex patterns
- Linguistic Structure Discovery
- Given set of sentences formed from words w $\in L$, discover set of subsequences $\Lambda$ that result in a more compact description of the structure
- Elements $\lambda \in \Lambda$ constitute a hierarchy, leaf nodes (POS) are subsets of $L$


## Semantics First: Objects / Nominals

## Language Grounding: Entity/Object

- object = coherent salient region in perceptual space
o object view schema [white maruti 800 from camera 1]
- object schema [white maruti 800]
- object category schema [car]
o bottom-up dynamic attention



## Language - Meaning Associaction

- Relative Association (bayesian)

$$
P\left(\gamma_{j} \mid \lambda_{i}\right)=\frac{P\left(\lambda_{i} \mid \gamma_{j}\right) P\left(\gamma_{j}\right)}{P\left(\lambda_{i}\right)} \propto \frac{P\left(\lambda_{i} \mid \gamma_{j}\right)}{P\left(\lambda_{i}\right)}
$$

- Mutual association (contribution to M.I.)

$$
\begin{gathered}
P\left(\lambda_{i}, \gamma_{j}\right) \log \frac{P\left(\lambda_{i}, \gamma_{j}\right)}{P\left(\lambda_{i}\right) P\left(\gamma_{j}\right)} \\
I(\Gamma, \Lambda)=\sum_{i} \sum_{j} P\left(\lambda_{i}, \gamma_{j}\right) \log \frac{P\left(\lambda_{i}, \gamma_{j}\right)}{P\left(\lambda_{i}\right) P\left(\gamma_{j}\right)}
\end{gathered}
$$

## Language Grounding: Nominals

| [BS] |  |  | [SS] |  |  | [C] |  |  |
| :--- | :---: | :---: | :--- | :---: | :---: | :--- | :---: | :---: |
| word(s) | $A_{i j}^{\text {rel }}$ | $A_{i j}^{\text {mut }}$ | word(s) | $A_{i j}^{\text {rel }}$ | $A_{i j}^{\text {mut }}$ | word(s) | $A_{i j}^{\text {rel }}$ | $A_{i j}^{\text {mut }}$ |
| square | 0.70 | 1.41 | little | 0.66 | 0.79 | circle | 0.79 | 2.11 |
| big | 0.89 | 1.11 | small | 0.72 | 0.63 | square | 0.41 | 1.54 |
| box | 0.69 | 0.78 | square | 0.46 | 1.12 | little | 0.68 | 1.22 |
| the big | 0.87 | 0.71 | small square | 0.93 | 0.53 | the little | 0.71 | 0.81 |
| big square | 0.94 | 0.75 | little square | 0.89 | 0.46 | little circle | 0.91 | 0.60 |
| large square | 0.86 | 0.15 | the little | 0.70 | 0.54 | the big | 0.48 | 0.61 |

# Perceptual Discovery : <br> Actions: Verbs 

## Perceptual Discovery: 2-agent actions

- Consider every pair of objects $A, B$ A : attended to object (tr)
B : other object (landmark, Im).
- 2 features suffice:
relative-velocity and relative position


$$
\text { pos•velDiff: }\left(\vec{x}_{B}-\vec{x}_{A}\right) \cdot\left(\vec{v}_{B}-\vec{v}_{A}\right)
$$

relative pose and the sum of the velocities

$$
\text { pos.velSum : }\left(\vec{x}_{B}-\vec{x}_{A}\right) \cdot\left(\vec{v}_{B}+\vec{v}_{A}\right)
$$

## Perceptual Discovery: 2-agent actions

- Static time-shots of feature space trajectories



## Switching the in-Focus agent

$\square$ Human Labels (CC, MA, Chase) $\rightarrow$ Ground Truth $\square$ Label Vs Cluster assigned


Number of Clusters from MNG $=4$ when Edge Aging $=30$ ( 0.9 prob)
CC: Come-Closer (C1), MA: Move Away (C2), $\mathrm{C}_{3} \& \mathrm{C}_{4}$ : Chase
Chase sub-categories:
Chase_RO-chases-LO: $\mathrm{C}_{3} \rightarrow$
Chase_LO-chases-RO: $\mathrm{C}_{4} \rightarrow$


## Hierarchy in Concept Space

$\square$ More clusters $\rightarrow$ Reveals category hierarchy:


Come-Closer-RO-static Come-Closer-LO-static
Come-Closer-both-moving
$\square$ Similarly: Move-Away : 3 subclasses
Number of Clusters from MNG = 8 when Edge Aging $=16$

|  | $C_{1}$ | $C_{2}$ | $C_{3}$ | $C_{4}$ | $C_{5}$ | $C_{6}$ | $C_{7}$ | $C_{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CC | 201 | 3 | 9 | 20 | 189 | 21 | 1 | 0 |
| MA | 8 | 126 | 4 | 45 | 9 | 1 | 181 | 6 |
| Chase | 1 | 9 | 142 | 151 | 13 | 9 | 32 | 26 |

$\mathrm{C}_{1}, \mathrm{C}_{5}, \mathrm{C}_{6}$ : sub-classes of Come-Closer; $\mathrm{C}_{2}, \mathrm{C}_{7}, \mathrm{C}_{8}$ :of Move-Away

## Two agent action ontology



## Learning verbs

| CLUSTER 1 |
| :---: | :---: | :---: | :---: |
| (Come-Close) |$\quad$| CLUSTER 2 |
| :---: |
| (Move-Away) |$\quad$| CLUSTER 3 |
| :---: |
| (Chase) |$\quad$| CLUSTER 4 |
| :---: |
| (Chase) |

ONE WORD LONG LINGUISTIC LABELS(MONOGRAMS)

| corner | 0.077 | $\\|$ | away | 0.069 | $\\|$ | chase | 0.671 |  | chase | 0.429 | $\square$ |
| :---: | :---: | :--- | :---: | :---: | :--- | :---: | :---: | :--- | :---: | :---: | :---: |
| move | 0.055 | $\\|$ | move | 0.055 | $\\|$ | other | 0.185 | $\square$ | after | 0.112 | $\square$ |
| attack | 0.042 | $\\|$ | chase | 0.049 | $\\|$ | around | 0.183 | $\square$ | out | 0.033 |  |

TWO WORD LONG LINGUISTIC LABELS(BIGRAMS)

| each other | 0.086 | $\square$ | move away | 0.111 | $\square$ | chase around | 0.306 |  | chase after | 0.218 | $\square$ |
| :---: | :---: | :--- | :---: | :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| move toward | 0.065 | $\square$ | go into | 0.035 |  | each other | 0.227 | $\square$ | just chase | 0.060 | $\square$ |
| toward each | 0.065 | $\square$ | into with | 0.035 |  | chase each | 0.198 | $\square$ | chase out | 0.058 | $\square$ |

THREE WORD LONG LINGUISTIC LABELS(TRIGRAMS)

| move toward each | 0.182 | $\square$ | go into with | 0.099 |  | chase each other | 0.558 |  | just chase out | 0.142 |
| :---: | :---: | :--- | :---: | :---: | :--- | :---: | :---: | :---: | :---: | :---: |
| toward each other | 0.182 | $\square$ | run away out | 0.051 |  | start run away | 0.132 | $\square$ | run away out | 0.047 |
| move close together | 0.114 | $\square$ | scare in corner | 0.032 |  | begin to move | 0.127 | $\square$ | to go after | 0.031 |

## Discovering Containment Relations : <br> Prepositions

## Clustering spatial relations

Feature Commitment:
Visual angle subtended at trajector by landmark


Histogram of visual subtended angle for the 3 shapes


## Clustering spatial relations

## IN cluster (emergent)

## 0 <br> 

VisAngle (Im at tr)


## Words for motions ending in / out



| IN | $A_{i j}^{\text {rel }}$ | $A_{i j}^{\text {mut }}$ | INTO | $A_{i j}^{\text {rel }}$ | $A_{i j}^{\text {mut }}$ | OUT OF | $A_{i j}^{\text {rel }}$ | $A_{i j}^{\text {mut }}$ |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| inside | 0.79 | 11.78 | into | 0.82 | 6.98 | out | 0.65 | 5.71 |
| into | 0.90 | 9.43 | inside | 0.53 | 1.03 | leaves | 1.00 | 4.16 |
| in | 0.61 | 4.16 | enters | 1.00 | 4.85 | exits | 1.00 | 3.46 |

## Syntax discovery and Semantic Association

## Syntax Discovery

- Syntactic discovery:
- Given input text, attempt to find graph that results in minimizing the description length
- Relational Graph RDS: patterns as nodes; edges as transitions
- Attempt to edit RDS to detect significant patterns
- Equivalence classes
 emerge at the nodes


## Computing the Image Schema

Our reflective baby has discovered:
"in" = label corresponding to this image schema
Hence: symbol for [IN] is
(note: this is an early, very basic, low-confidence characterization


## Language Structures : Verbs

1. $\left[\begin{array}{c}\text { the } \rightarrow\left[\begin{array}{c}\text { big } \\ \text { large } \\ \text { the } \rightarrow \text { square }\end{array}\right] \rightarrow \text { square }\end{array}\right] \rightarrow\left[\begin{array}{c}\text { scares } \\ \text { approaches } \\ \text { chases }\end{array}\right] \rightarrow\left[\right.$ the $\left.\rightarrow\left[\begin{array}{l}\text { small } \\ \text { little }\end{array}\right]\right]$
2. $\left[\begin{array}{c}\text { the } \rightarrow\left[\begin{array}{c}\text { ball } \\ \text { box } \\ \text { door } \\ \text { square }\end{array}\right] \\ \text { circle } \\ \text { it }\end{array}\right] \rightarrow\left[\begin{array}{c}\text { moved } \\ \text { moves } \\ \text { runs }\end{array}\right]$

ADIOS [solan / edelman 05]

## Hindi Acquisition: Word learning

| [BS] |  | [SS] |  |  | [C] |  |  | [IN] |  |  |
| :--- | :---: | :---: | :--- | :---: | :---: | :--- | :--- | :--- | :--- | :--- |
| word(s) | $A_{i j}^{r e l}$ | $A_{i j}^{m}$ | word(s) | $A_{i j}^{r e l}$ | $A_{i j}^{m}$ | word(s) | $A_{i j}^{\text {rel }}$ | $A_{i j}^{m}$ | word(s) | $A_{i j}^{r e l}$ |$A_{i j}^{m}$.

## Incipient Syntax



## Scaling up?

- Domain-specific grammar
- After learning several such grammars for different domains, how to merge?


## Conclusion

## The power of Latent Discovery

- Data is not randomly drawn
- Discovering implicit strucgture in data $\rightarrow$
- Tacit Knowledge
- Much work remains in scaling up
- How to merge diverse domains?
-Learning to plan motions
- Learn low-dimensional representations of motion
- Learning Language / Vision


## Humans and Robots



